## Chapter 4 <br> Section 4.5 <br> Word Problems

1. A company manufactures baseball caps with school logos. The company charges their customers a fixed fee of $\$ 500$ for setting up the machines and $\$ 8$ for each cap produced.
(a) Find a linear model for the cost of purchasing any number of caps from this company. Express this model as a function.
(b) Use the model to find the cost of purchasing 225 caps.
(c) Use the model to find the number of caps sold if the customer pays $\$ 2100$.
2. The average U.S. resident uses 650 lb of paper a year. The average pine tree produces 4130 lb of paper.
(a) Find a function $N$ that models the number of trees used for paper in one year by $x$ U.S. residents.
(b) The city of Cleveland Heights, Ohio, had a population of 49,000 in 2003. Use the model to find the number of trees required to make the paper used by the residents of Cleveland Heights in 2003.
(c) Use the model to determine how many U.S. residents can be supplied with paper for a year from 200 pine trees.
3. A gardener waters his vegetble plot using a drip irrigation system. Water flows slowly from a 1200-gallon tank through a perforated hose network to keep the soil appropriately moist. During the spring planting season, the garden requires 80 gallons of water per day.
(a) Find a function $W$ that gives the amount of water in the tank $x$ days after it has been filled.
(b) Use the function $W$ to find the water remaining in the tank after 3 days and after 12 days.
(c) Calculate $W(20)$. What does this answer tell you?
(d) How many days will it take for the tank to empty?
(e) The gardener prefers not to let the tank empty completely. Instead, he decides to refill it when the water level has dropped to 200 gallons. How many days should he wait to refill the tank and how many gallons of water will he need?
4. A breakfast cereal company manufactures boxes to package their product. For aesthetic reasons, the box must have the following proportions: Its width is 3 times its depth, and its height is 5 times its depth.
(a) Why might a cereal company have aesthetic reasons for the dimensions of its box?
(b) Find a function that models the volume of the box in terms of its depth, and graph the function.
(c) Find the volume of the box if the depth is 1.5 in.
(d) For what depth is the volume $90 \mathrm{in}^{3}$ ?
(e) For what depth is the volume greater than $60 \mathrm{in}^{3}$ ?
5. A gardener has 140 ft of fencing to fence a rectangular vegetable garden.
(a) Find a function that models the area of the garden she can fence with respect to the width.
(b) For what range of widths is the area greater than $825 \mathrm{ft}^{2}$ ?
(c) Can she fence a garden with area $1250 \mathrm{ft}^{2}$ ?
(d) Find the dimensions of the largest area she can fence.
